

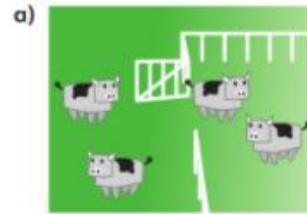
# Simplifying fractions 1

## Discover



- 1 a) Bella gets 2 cows into the pen before the time runs out.  
What is her score? Give your answer as a fraction in its simplest form.
- b) Lee gets 9 of the 12 sheep into the pen.  
What is his score? Give your answer as a fraction in its simplest form.

## Share



To find a fraction's simplest form we divide the numerator and the denominator by a **common factor**.



Bella's score is 2 out of 4.

We can write this fraction as  $\frac{2}{4}$ .



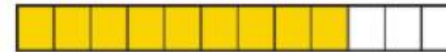
$$\begin{array}{c} \div 2 \\ \downarrow \\ \frac{2}{4} = \frac{1}{2} \\ \uparrow \\ \div 2 \end{array}$$

I divided the numerator and denominator by 2 because 2 is a common factor of 2 and 4.



$\frac{2}{4}$  can be simplified to  $\frac{1}{2}$ . Bella's score is  $\frac{1}{2}$ .

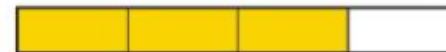
- b) Lee gets  $\frac{9}{12}$  of the sheep in the pen.



We can divide the numerator and the denominator by 3 because 3 is a common factor of 9 and 12.

$$\begin{array}{c} \div 3 \\ \downarrow \\ \frac{9}{12} = \frac{3}{4} \\ \uparrow \\ \div 3 \end{array}$$

These fractions represent the same amount, but one is written in its simplest form.

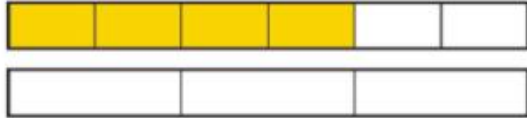


Lee's score is  $\frac{3}{4}$ .

## Think together

- 1 Bella and Lee play some more rounds of the game. What scores do they get? Use the diagrams to help you simplify the fractions.

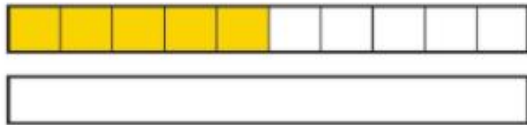
- a) Bella gets 4 out of 6 sheep in the pen.



$$\frac{4}{6} = \frac{\square}{3}$$

Diagram showing a fraction  $\frac{4}{6}$  with a box in the numerator. A curved arrow above the fraction indicates dividing both numerator and denominator by 2. A curved arrow below the fraction indicates dividing both numerator and denominator by 2.

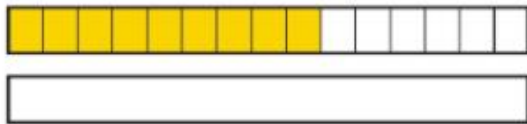
- b) Lee gets 5 out of 10 cows in the pen.



$$\frac{5}{10} = \frac{\square}{\square}$$

Diagram showing a fraction  $\frac{5}{10}$  with a box in the numerator and a box in the denominator. A curved arrow above the fraction indicates dividing both numerator and denominator by 5. A curved arrow below the fraction indicates dividing both numerator and denominator by 5.

- c) Bella gets 9 out of 15 geese in the pen.



$$\frac{9}{15} = \frac{\square}{\square}$$

Diagram showing a fraction  $\frac{9}{15}$  with a box in the numerator and a box in the denominator. A curved arrow above the fraction indicates dividing both numerator and denominator by 3. A curved arrow below the fraction indicates dividing both numerator and denominator by 3.

- 2 Simplify these fractions.

a)  $\frac{6}{8}$

b)  $\frac{10}{100}$

c)  $\frac{7}{7}$

- 3 a) Use your knowledge of equivalent fractions to find the missing numbers.

$$\frac{5}{6} = \frac{10}{\square}$$

Diagram showing a fraction  $\frac{5}{6}$  with a box in the denominator. A curved arrow above the fraction indicates multiplying both numerator and denominator by 2. A curved arrow below the fraction indicates multiplying both numerator and denominator by 2.

$$\frac{3}{10} = \frac{15}{\square}$$

Equivalent means equal to.



- b) Fill in the missing numbers to make the simplified fractions correct.

$$\frac{15 + 5}{29 + 6} = \frac{\square}{\square}$$

$$\frac{\square + 19}{30} = \frac{5}{6}$$

$$\frac{25 - \square}{28} = \frac{3}{4}$$

$$\frac{\square + 15}{20} = \frac{4}{\square}$$

I remember how to find equivalent fractions. I need to multiply the numerator and denominator by the same number.



# Simplifying fractions 2

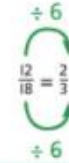
## Discover



- a) What fraction of the people are children?  
Simplify your answer.
- b) How many roller coaster carriages are full?  
Simplify your answer.

## Share

- a) 12 children: factors of 12 are 1, 2, 3, 4, **6** and 12  
18 people: factors of 18 are 1, 2, 3, **6**, 9, 18



Divide the numerator and denominator by 6.



The **highest common factor** of 12 and 18 is 6. This is the highest number that divides into both 12 and 18.



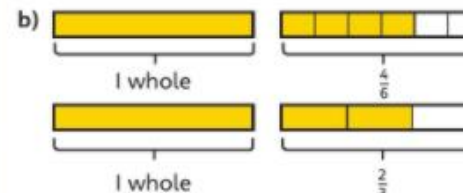
I did it a different way. I know that 12 and 18 can both be divided by 2 so I started by doing that. I then noticed I could divide the answer by 3.

Divide the numerator and denominator by 2.



6 and 9 have a common factor of 3.  
Divide the numerator and denominator by 3.

$\frac{2}{3}$  of the people are children.



1 carriage is full and the other is  $\frac{4}{6}$  full.

To simplify  $1\frac{4}{6}$  we keep the whole number the same and simplify the fraction.

$1\frac{4}{6}$  simplifies to  $1\frac{2}{3}$ .

$1\frac{2}{3}$  roller coaster carriages are full.


We know we have simplified fully when we cannot divide the numerator and denominator by any other number apart from 1.




## Think together

- 1 a) Olivia wants to go on the ghost train. Three of the carriages are full. In the remaining carriage, 8 out of 10 seats are taken.

Simplify  $3\frac{8}{10}$



$\div 2$



$\frac{8}{10} = \frac{\square}{\square}$

$\div 2$

So  $3\frac{8}{10} = \square\frac{\square}{\square}$

- b) When she gets off the train after her ride, she counts 25 people waiting. Each carriage has 10 seats.

How many carriages will be full? Simplify your answer.



$$\frac{25}{10} = \square\frac{\square}{10} = \square\frac{\square}{\square}$$

- 2 Some children are trying to fully simplify  $16\frac{8}{24}$ .

They all use a different method. Which children have used correct methods? Explain how you know.

The highest common factor of 16, 8 and 24 is 8, so I divided all the numbers by 8.

Olivia

I kept the whole number the same and divided the numerator and denominator by the highest common factor of 8.

Lexi

I kept the whole number the same and divided the numerator and denominator by 4.

Isla

I divided all the numbers by 2, then by 2 again, then by 2 again.

Amelia

I divided the numerator and denominator by 2, then by 4, but kept the whole number the same.

Emma

- 3 Which is bigger:

$$\frac{288}{160} \text{ or } \frac{9}{5}?$$

Explain how you know.

I will simplify the fractions before I compare them.

I wonder what is the best way to simplify the fractions.



CHALLENGE

# Fractions on a number line



## Discover

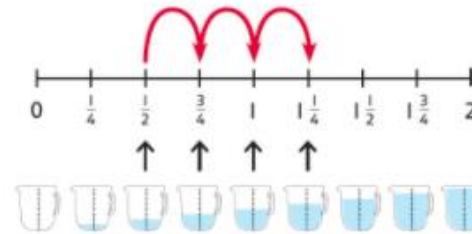


- 1 a) The ceiling on Max's side of the room drips  $\frac{1}{4}$  litre of water every hour. Max has already collected  $\frac{1}{2}$  a litre of water in his jug. How many litres of water will be in his jug after another 3 hours?
- b) Max collects  $5\frac{3}{4}$  litres of water in total. His dad collects  $5\frac{4}{5}$  litres of water in total. Use a number line to show who collected the most water.

## Share



- a) Max's jug contains  $\frac{1}{2}$  litre of water to start with. Starting from  $\frac{1}{2}$  we can count up in quarters ( $\frac{1}{4}$ ).



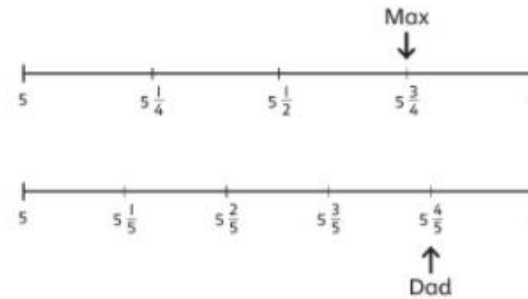
I counted up  $\frac{1}{4}$  three times.



There will be  $1\frac{1}{4}$  litres of water in Max's jug after another 3 hours.

- b) Both amounts of water lie between 5 and 6.

We can compare number lines divided into quarters and fifths.



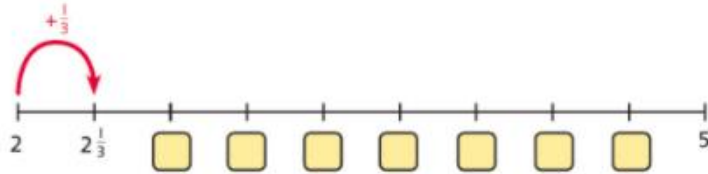
I put my number lines together to help me compare.



$5\frac{4}{5}$  is bigger than  $5\frac{3}{4}$  so Max's dad collected the most water.

## Think together

- 1 Danny is running a bath. There are 2 litres of water in the bath already. It fills up at a rate of  $\frac{1}{3}$  litre each second. How many litres are in the bath after 8 seconds?



There are   litres of water in the bath after 8 seconds.

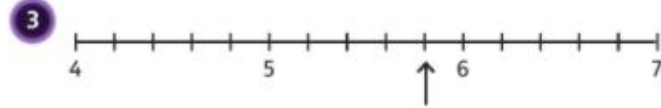
- 2 a) What numbers are missing from the number line?



- b) What numbers are missing from the number line?



- c) Danny is counting up from 1 to 3 in jumps of  $\frac{2}{6}$ . Complete the jumps and fill in the missing numbers.



- a) What number is the arrow pointing to?  
 b) What is  $\frac{2}{5}$  more than the number the arrow is pointing to?  
 c) What is  $\frac{1}{5}$  less than the number the arrow is pointing to?  
 d) What is 1 more than the number the arrow is pointing to?

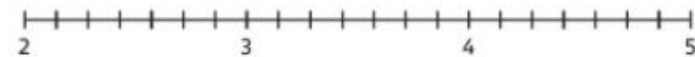
- 4 a) Find where these numbers should go on the number line.

$$2\frac{3}{10} \quad 2\frac{1}{2} \quad 2\frac{9}{10}$$



- b) This sequence goes up by the same amount each time. Use the number line to help you work out the missing fractions.

$$\square, 3\frac{1}{7}, \square, \square, 4\frac{3}{7}, \square$$



I used the number line and looked at the gaps between the numbers.



CHALLENGE

# Comparing and ordering fractions 1

## Discover



Group A

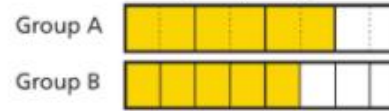
Group B

- 1 a) Which group has a bigger fraction of people wearing glasses?
- b) Some more people are in Group C.  $\frac{2}{3}$  of the people in Group C are wearing glasses.  
Which group now has the biggest fraction of people wearing glasses?



## Share

- a) We need to compare  $\frac{3}{4}$  and  $\frac{5}{8}$ .



$\frac{3}{4}$  is equivalent to  $\frac{6}{8}$ .

$$\begin{array}{c} \times 2 \\ \frac{3}{4} = \frac{6}{8} \\ \times 2 \end{array}$$



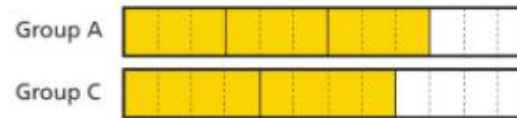
I found equivalent fractions for Group A so that I could compare  $\frac{1}{8}$ s.



$\frac{6}{8}$  is greater than  $\frac{5}{8}$  so  $\frac{3}{4}$  is greater than  $\frac{5}{8}$ .

Group A has a bigger fraction of people wearing glasses.

- b) Now we need to compare  $\frac{3}{4}$  and  $\frac{2}{3}$ .



Multiples of 4 are 4, 8, 12.

Multiples of 3 are 3, 6, 9, 12.

The lowest common multiple of 4 and 3 is 12 so we can find equivalent fractions with a denominator of 12.

$$\begin{array}{c} \times 3 \\ \frac{3}{4} = \frac{9}{12} \\ \times 3 \end{array} \quad \begin{array}{c} \times 4 \\ \frac{2}{3} = \frac{8}{12} \\ \times 4 \end{array}$$

$\frac{9}{12} > \frac{8}{12}$  so  $\frac{3}{4} > \frac{2}{3}$

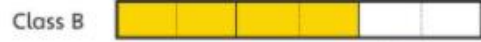
I needed to find equivalent fractions for both groups. To get the same denominator I found the **lowest common multiple (LCM)** of 4 and 3.



Group A has the biggest fraction of people wearing glasses.

## Think together

- 1 a)  $\frac{5}{6}$  of Class A have brown hair.  $\frac{2}{3}$  of Class B have brown hair. Which class has a bigger fraction of children with brown hair?



The LCM of 6 and 3 is .  $\frac{2}{3} = \frac{\text{input}}{6}$   $\frac{5}{6} \text{ } \text{input} \frac{\text{input}}{6}$  so  $\frac{5}{6} \text{ } \text{input} \frac{2}{3}$ .  
Class  has a bigger fraction of children with brown hair.

- b)  $\frac{1}{2}$  of Class A has a pet.  $\frac{3}{8}$  of Class B have a pet.

Which class has a bigger fraction of children with a pet?



The LCM of 2 and 8 is .  $\frac{1}{2} = \frac{\text{input}}{\text{input}}$   $\frac{1}{2} \text{ } \text{input} \frac{3}{8}$   
Class  has a bigger fraction of children with a pet.

- c)  $\frac{3}{5}$  of Class A are girls.  $\frac{2}{3}$  of Class B are girls.

Which class has a bigger fraction of girls?

The LCM of 5 and 3 is .

$$\frac{3}{5} = \frac{\text{input}}{\text{input}} \quad \frac{2}{3} = \frac{\text{input}}{\text{input}} \quad \frac{3}{5} \text{ } \text{input} \frac{2}{3}$$

Class  has a bigger fraction of girls.

- 2 Put each of these sets of fractions in order from smallest to biggest.

a)  $\frac{2}{3}, \frac{1}{2}, \frac{5}{6}$

b)  $\frac{1}{2}, \frac{5}{12}, \frac{5}{6}, \frac{3}{4}$

c)  $\frac{4}{5}, \frac{3}{10}, \frac{49}{50}, \frac{4}{4}, \frac{99}{100}$

I need to find the lowest common multiple of more than two numbers here. This will be the denominator that I need to use in order to compare.



- 3 Fill in the missing digits to make the statements correct.

a)  $\frac{\text{input}}{6}$  is bigger than  $\frac{2}{3}$

d)  $\frac{\text{input}}{5} > \frac{1}{2} > \frac{\text{input}}{10}$

b)  $\frac{2}{5}$  is smaller than  $\frac{\text{input}}{15}$

e)  $\frac{3}{8} < \frac{\text{input}}{6}$

c)  $\frac{1}{3} > \frac{\text{input}}{4}$

f)  $\frac{3}{\text{input}} < \frac{\text{input}}{3}$

I think some statements may have more than one answer.

I can use a fraction wall or fraction strips to help me.



## Comparing and ordering fractions 2

### Discover



My cat eats  $1\frac{3}{5}$  pouches of cat food each day.

Bella

My cat eats  $1\frac{2}{3}$  pouches of cat food each day.

Jamie

- 1 a) Does Bella's cat eat more than Jamie's cat each day?
- b) Ebo's cat eats  $1\frac{4}{7}$  pouches of cat food each day.  
Does Ebo's cat eat more than Bella's cat?

### Share

- a) Bella's cat    
 Jamie's cat  

I need to compare  $1\frac{3}{5}$  and  $1\frac{2}{3}$ . I think I only need to compare the fractions.

To compare  $1\frac{3}{5}$  and  $1\frac{2}{3}$  I need to find the **lowest common denominator**.

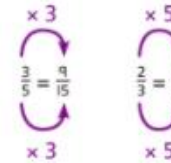
Multiples of 5 are 5, 10, **15**.

Multiples of 3 are 3, 6, 9, 12, **15**.

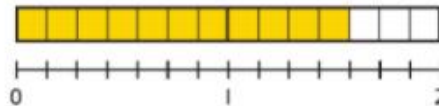
The lowest common denominator is 15.

$$\frac{9}{15} < \frac{10}{15} \text{ so } \frac{3}{5} < \frac{2}{3}$$

$1\frac{3}{5}$  is less than  $1\frac{2}{3}$  so Bella's cat does not eat more than Jamie's cat each day.



- b) We need to compare  $1\frac{3}{5}$  and  $1\frac{4}{7}$ .



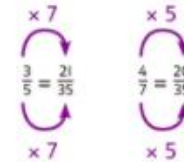
I converted  $1\frac{4}{7}$  to  $1\frac{4}{7}$  so they are easier to compare.

The whole numbers are the same so we only need to compare  $\frac{3}{5}$  and  $\frac{4}{7}$ .

The lowest common denominator is 35.

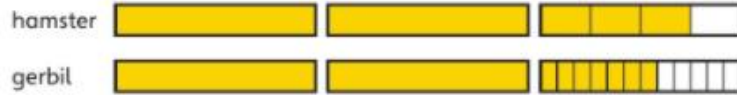
$$\frac{21}{35} > \frac{20}{35} \text{ so } \frac{3}{5} > \frac{4}{7} \text{ so } 1\frac{3}{5} > 1\frac{4}{7}$$

$1\frac{4}{7} < 1\frac{3}{5}$  so Ebo's cat does not eat more than Bella's cat.



## Think together

- 1 a) Lexi's hamster eats  $2\frac{3}{4}$  bowls of food each week. Her gerbil eats  $2\frac{7}{12}$  bowls of food each week. Which animal eats more each week?



$$\frac{3}{4} = \frac{\square}{12}$$

$$\text{So } 2\frac{3}{4} = 2\frac{\square}{12}$$

$$2\frac{3}{4} \text{ (blue circle)} < 2\frac{7}{12}$$

Lexi's \_\_\_\_\_ eats more each week.

- b) There are 8 carrots in a bag. Roxy the horse eats 27 carrots per week.

How many bags of carrots does she eat per week?

$$\frac{\square}{8} = \frac{\square}{8}$$

Roxy eats  $\frac{\square}{8}$  bags of carrots per week.

- c) Mai the horse eats  $3\frac{1}{2}$  bags of carrots per week.

Which horse eats more carrots per week?

$$3\frac{1}{2} = 3\frac{\square}{8} \quad \frac{\square}{8} \text{ (blue circle)} < 3\frac{\square}{8}$$

\_\_\_\_\_ eats more carrots per week.

- 2 Max has four fraction cards.



Which fraction is the biggest?

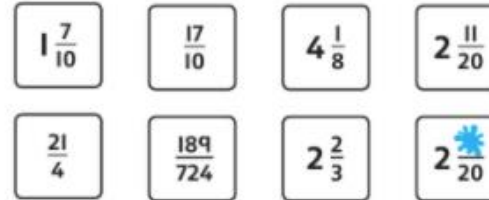
Put the fractions in ascending order.

- 3 Jamilla has some fraction cards.

$$2\frac{3}{5}$$

She selects the following fraction card.

Which fraction cards are bigger than Jamilla's?



Some of these are clearly bigger. I can tell by just looking.

The last card is bigger than Jamilla's number. I wonder what number could be missing.



CHALLENGE

# Adding and subtracting fractions 1

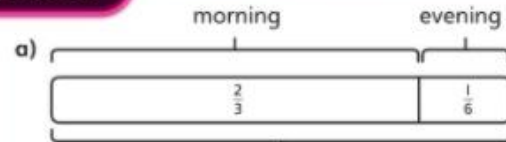
## Discover



I need to feed Hattie  $\frac{2}{3}$  of a bale of hay in the morning and  $\frac{1}{6}$  in the evening.

- 1 a) What fraction of a bale of hay does Hattie eat in a day?
- b) Molly eats  $\frac{1}{4}$  of a bale of hay less than Hattie per day.  
What fraction of a bale of hay does Molly eat in a day?

## Share



When adding or subtracting fractions, we need to find a common denominator.

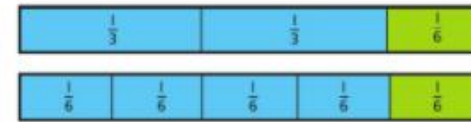


Multiples of 3 are 3, **6**.

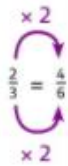
A multiple of 6 is **6**.

The lowest common multiple of 3 and 6 is 6.

I will find an equivalent fraction with a denominator of 6.



$$\frac{2}{3} + \frac{1}{6} = \frac{4}{6} + \frac{1}{6} = \frac{5}{6}$$



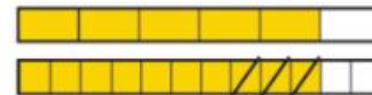
Hattie eats  $\frac{5}{6}$  of a bale of hay in a day.

- b) Molly eats  $\frac{1}{4}$  of a bale less than Hattie.

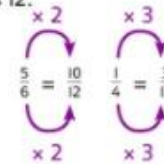
Use the LCM of 6 and 4 to find a common denominator.

Multiples of 6 are 6, **12**

Multiples of 4 are 4, 8, **12** The LCM is 12.



$$\frac{5}{6} - \frac{1}{4} = \frac{10}{12} - \frac{3}{12} = \frac{7}{12}$$



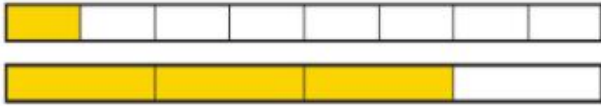
Molly eats  $\frac{7}{12}$  of a bale of hay in a day.

I need to subtract.



## Think together

- 1 a) Hector eats  $\frac{1}{8}$  of a bale of hay in the morning and  $\frac{3}{4}$  of a bale of hay in the evening. How much hay does he eat in a day?



The LCM of 8 and 4 is . So  $\frac{3}{4} = \frac{\text{input}}{8}$

$$\frac{1}{8} + \frac{\text{input}}{8} = \frac{\text{input}}{8}$$

Hector eats  of a bale of hay in a day.

- b) Callie eats  $\frac{2}{3}$  of a bale of hay. Scoobie eats  $\frac{5}{9}$  less. How much does Scoobie eat?



The LCM of 3 and 9 is .  $\frac{2}{3} = \frac{\text{input}}{\text{input}}$

$$\frac{\text{input}}{\text{input}} - \frac{\text{input}}{\text{input}} = \frac{\text{input}}{\text{input}}$$

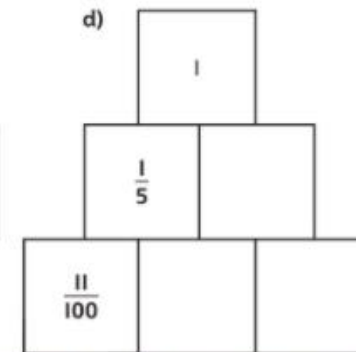
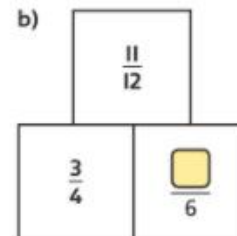
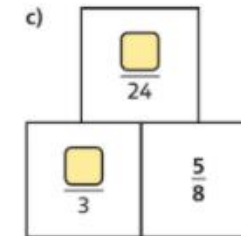
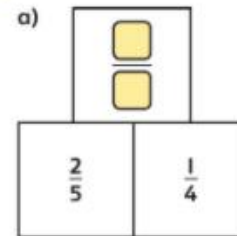
Scoobie eats  of a bale of hay.

- 2 Work out  $\frac{1}{6} + \frac{3}{8}$ .

The LCM of 6 and 8 is .

$$\frac{1}{6} = \frac{\text{input}}{\text{input}} \quad \frac{3}{8} = \frac{\text{input}}{\text{input}} \quad \frac{\text{input}}{\text{input}} + \frac{\text{input}}{\text{input}} = \frac{\text{input}}{\text{input}}$$

- 3 Complete the following addition pyramids.



CHALLENGE



I think I might need to subtract to find some of the missing fractions.

I think it would help to think about common denominators.



## Adding and subtracting fractions 2

### Discover



- 1** a) On Saturday, Amelia cycles  $3\frac{2}{5}$  kilometres with her dad.  
On Sunday, she cycles  $1\frac{1}{3}$  kilometres.  
How many kilometres does Amelia cycle in total?
- b) How many more kilometres does Amelia cycle on Saturday than on Sunday?

### Share

a) Saturday



Sunday



Add the wholes:



$$3 + 1 = 4$$

Add the parts:

$$\frac{2}{5} + \frac{1}{3}$$

Multiples of 5 are 5, 10, **15**

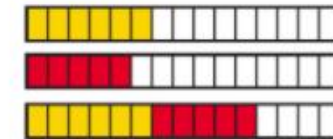
Multiples of 3 are 3, 6, 9, 12, **15**

The lowest common multiple is 15.

So

$$\frac{2}{5} + \frac{1}{3} = \frac{6}{15} + \frac{5}{15} = \frac{11}{15}$$

Amelia cycles  $4 + \frac{11}{15} = 4\frac{11}{15}$  in total.



b) We need to subtract to find the difference.

$$3\frac{2}{5} - 1\frac{1}{3}$$

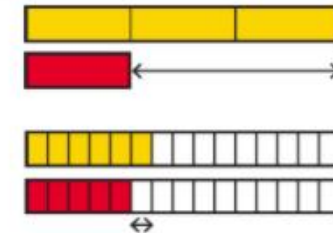
First subtract the wholes.

$$3 - 1 = 2$$

Then subtract the parts.

$$\frac{2}{5} - \frac{1}{3} = \frac{6}{15} - \frac{5}{15} = \frac{1}{15}$$

So Amelia cycles  $2\frac{1}{15}$  more km on Saturday than on Sunday.



## Think together

- 1 a) Luis walks  $2\frac{1}{4}$  kilometres on Saturday and  $2\frac{3}{8}$  kilometres on Sunday.



How far does Luis walk in total?

Add the wholes:  $2 + 2 = \square$

Add the parts:  $\frac{1}{4} = \frac{\square}{8}$      $\frac{1}{4} + \frac{3}{8} = \frac{\square}{8} + \frac{3}{8} = \frac{\square}{8}$

$2\frac{1}{4} + 2\frac{3}{8} = \square\frac{\square}{8}$  so Luis walks  $\square\frac{\square}{8}$  kilometres in total.

- b) Jamie swims  $5\frac{1}{2}$  lengths of a swimming pool.

Ambika swims  $3\frac{2}{5}$  lengths of the swimming pool.

How many more lengths does Jamie swim than Ambika?

$\square - \square = \square$

$\frac{1}{2} = \frac{\square}{5}$      $\frac{2}{5} = \frac{\square}{5}$      $\frac{1}{2} - \frac{2}{5} = \frac{\square}{5} - \frac{\square}{5} = \frac{\square}{5}$

$5\frac{1}{2} - 3\frac{2}{5} = \square\frac{\square}{5}$  so Jamie swims  $\square\frac{\square}{5}$  more lengths than Ambika.

- 2 Find the missing values.

a) 

?	
$9\frac{1}{6}$	$7\frac{5}{8}$

b) 

$4\frac{2}{3}$	
?	$\frac{2}{7}$

- 3 Richard's dad has a model railway, with a train track  $2\frac{3}{4}$  metres long.

He buys a second train track.

This train track is  $\frac{3}{5}$  metres shorter than the first one.

The tracks are put together to make a longer track.

How long is the new train track?



I think I need to do an addition and subtraction in this calculation.



I only have two fractions though.



## Adding fractions

### Discover



There are  $2\frac{3}{4}$  tonnes of carrots on one trailer and  $1\frac{1}{2}$  tonnes on the other.



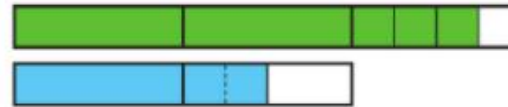
- 1** a) What is the total weight of carrots the farmer has harvested so far?
- b) A supermarket orders 5 tonnes of carrots.  
The farmer harvests another  $\frac{4}{5}$  tonnes of carrots from a different field.  
Has the farmer harvested enough carrots to fulfil the order?

### Share



- a) We need to find  $2\frac{3}{4} + 1\frac{1}{2}$ .

#### Method 1



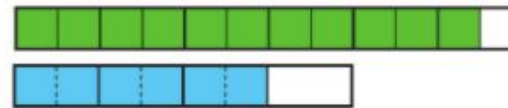
Add the wholes:  $2 + 1 = 3$

Add the parts:  $\frac{3}{4} + \frac{1}{2} = \frac{3}{4} + \frac{2}{4} = \frac{5}{4}$

$$\frac{5}{4} = 1\frac{1}{4}$$

So  $2\frac{3}{4} + 1\frac{1}{2} = 3 + 1\frac{1}{4} = 4\frac{1}{4}$

#### Method 2



$$2 = \frac{8}{4} \qquad 1\frac{1}{2} = \frac{3}{2} = \frac{6}{4}$$

$$\text{So } 2\frac{3}{4} + 1\frac{1}{2} = \frac{8}{4} + \frac{6}{4} \\ = \frac{14}{4} = 3\frac{2}{4} = 3\frac{1}{2}$$

The total weight of carrots the farmer has harvested so far is  $4\frac{1}{4}$  tonnes.

- b) Now we need to add  $4\frac{1}{4} + \frac{4}{5}$ .

Add the wholes:  $4 + 0 = 4$

Add the parts:  $\frac{1}{4} + \frac{4}{5} = \frac{5}{20} + \frac{16}{20} = \frac{21}{20} = 1\frac{1}{20}$

So  $4\frac{1}{4} + \frac{4}{5} = 4 + 1\frac{1}{20} = 5\frac{1}{20}$ .

$5\frac{1}{20}$  tonnes > 5 tonnes so the farmer has harvested enough carrots to fulfil the order.

I made the improper fraction into a mixed number and then put the answers together.



I changed the mixed numbers to improper fractions first, then added them together.



## Think together

1 Calculate  $1\frac{2}{3} + 2\frac{1}{2}$ .



a) Method 1

Add the wholes:  $1 + 2 =$

Add the parts:  $\frac{2}{3} + \frac{1}{2} =$   +  =

=  +

Add them together:  $1\frac{2}{3} + 2\frac{1}{2} =$   +  =

b) Method 2



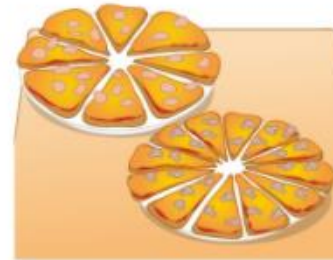
Change to improper fractions:  $1\frac{2}{3} =$    $2\frac{1}{2} =$

Now add the fractions:  $\frac{\text{input}}{3} + \frac{\text{input}}{2} =$   +  =

Change to a mixed number:  $\frac{\text{input}}{\text{input}} =$

2

chicken



mushroom

At a pizza buffet, 3 whole chicken pizzas and 7 slices were eaten.

Also, 4 whole mushroom pizzas and 5 slices were eaten.

How many pizzas were eaten altogether?

3

Here are some numbers.

$7\frac{3}{4}$    
   $4\frac{2}{3}$    
   $3\frac{5}{6}$    
   $6\frac{7}{8}$    
   $27\frac{17}{24}$

a) Isla adds two of the numbers together.

Her answer is  $11\frac{13}{24}$ .

Which two numbers did she choose?

b) What method would you use to add  $7\frac{3}{4}$  and  $27\frac{17}{24}$ ?

Explain your method.



I prefer to convert to improper fractions.



I am not sure what is the best method.

# Subtracting fractions

## Discover



I wonder how many more cups of cherries I need. I need to find  $3\frac{1}{3} - 1\frac{1}{2}$ .

I cannot find  $3\frac{1}{3} - 1\frac{1}{2}$  because  $\frac{1}{3}$  is less than  $\frac{1}{2}$ .



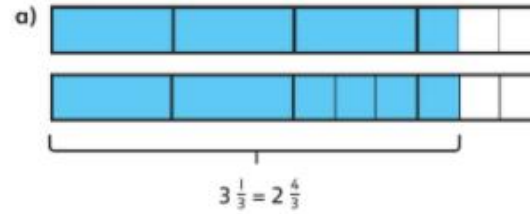
Max

Isla

You can do the subtraction if you change both numbers to improper fractions.

- 1 a) Is Max correct?
- b) Show how Isla's method will give you the answer to  $3\frac{1}{3} - 1\frac{1}{2}$ .

## Share



Subtract the wholes:  $2 - 1 = 1$

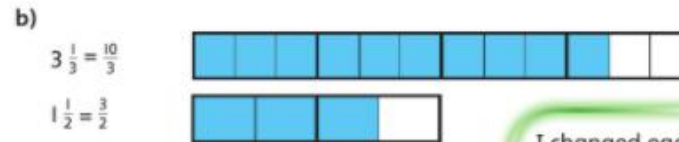
The lowest common multiple of 2 and 3 is 6.

Subtract the parts:  $\frac{4}{3} - \frac{1}{2} = \frac{8}{6} - \frac{3}{6} = \frac{5}{6}$

$$1 + \frac{5}{6} = 1\frac{5}{6}$$



Max is not correct - he can do the subtraction. He needs  $1\frac{5}{6}$  more cups of cherries.



$3\frac{1}{3} - 1\frac{1}{2}$  can be written as  $\frac{10}{3} - \frac{3}{2}$

$$\frac{10}{3} - \frac{3}{2} = \frac{20}{6} - \frac{9}{6} = \frac{11}{6}$$

Change back to a mixed number:  $\frac{11}{6} = 1\frac{5}{6}$

I changed each number to an improper fraction.

I needed to find  $3\frac{1}{3} - 1\frac{1}{2}$ . I rewrote  $3\frac{1}{3}$  as  $2\frac{4}{3}$  to make the fraction part bigger than  $\frac{1}{2}$  so it was easier to subtract.



## Think together

- 1 a) Work out  $4\frac{1}{3} - 2\frac{3}{4}$ .



Use the diagram to help you explain the method.



$$4\frac{1}{3} = 3 + 1\frac{1}{3} = 3\frac{\square}{3}$$

Subtract the wholes:  $3 - 2 = \square$

The lowest common multiple of 3 and 4 is  $\square$ .

Subtract the parts:

$$\frac{4}{3} - \frac{3}{4} = \frac{\square}{\square} - \frac{\square}{\square} = \frac{\square}{\square}$$



$$\text{So } 4\frac{1}{3} - 2\frac{3}{4} = \square + \frac{\square}{\square} = \square\frac{\square}{\square}$$

- b) Work out  $3\frac{1}{5} - 1\frac{1}{2}$  by converting each mixed number to an improper fraction.

$$3\frac{1}{5} = \frac{\square}{5} \quad 1\frac{1}{2} = \frac{\square}{2} \quad \text{so } 3\frac{1}{5} - 1\frac{1}{2} \text{ can be written as } \frac{\square}{5} - \frac{\square}{2}$$

The lowest common multiple of 5 and 2 is  $\square$ .

$$\text{Find a common denominator: } \frac{\square}{5} - \frac{\square}{2} = \frac{\square}{\square} - \frac{\square}{\square} = \frac{\square}{\square}$$

$$\text{Change back to a mixed number: } \frac{\square}{\square} = \square\frac{\square}{\square}$$

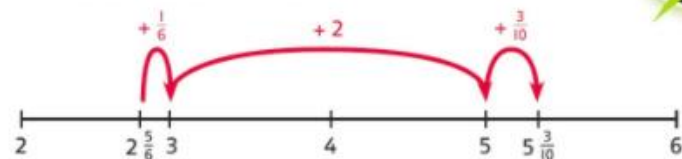
- 2 It takes Jamilla  $2\frac{1}{4}$  hours to complete a puzzle.

It takes Andy  $\frac{2}{3}$  of an hour less.

How many hours does it take Andy to complete the puzzle?

- 3 a) Danny is working out  $5\frac{3}{10} - 2\frac{5}{6}$ .

He counts on a number line.



What answer will Danny get using this method?

To find the answer using Danny's method, I will add the fractions and then the whole number.



- b) Use Max's, Isla's and Danny's methods to work out  $3\frac{1}{2} - 1\frac{7}{10}$  and  $26\frac{1}{2} - 18\frac{4}{5}$ .

I wonder which method is most efficient when the whole numbers are big.



## Problem solving – adding and subtracting fractions 1



### Discover



**Instructions to make purple paint**

- $1\frac{1}{2}$  litres of blue paint
- $2\frac{3}{4}$  litres of red paint
- $\frac{3}{4}$  litres of white paint

- 1** a) The children are going to make some purple paint using the instructions.  
How many litres of purple paint will they make?
- b)  $3\frac{1}{2}$  litres of purple paint are needed to fully cover all the roofs.  
 $1\frac{1}{5}$  litres of purple paint are needed to paint the wooden poles.  
Will there be enough paint to paint both the roofs and the poles?

### Share



I added the red and blue paint first and then added the white paint.

**Method 1**

Add the red point and blue point:  $2\frac{3}{5} + 1\frac{1}{2}$

Add the wholes:  $2 + 1 = 3$

The lowest common denominator of 5 and 2 is 10.

Add the fractions:  $\frac{3}{5} + \frac{1}{2} = \frac{6}{10} + \frac{5}{10} = \frac{11}{10} = 1\frac{1}{10}$

So  $3 + 1\frac{1}{10} = 4\frac{1}{10}$

Now add on the white point:  $4\frac{1}{10} + \frac{3}{4} = 4\frac{2}{20} + \frac{15}{20} = 4\frac{17}{20}$

The total paint made is  $4\frac{17}{20}$ .

**Method 2**

$2\frac{3}{5} + 1\frac{1}{2} + \frac{3}{4}$

Add the wholes:  $2 + 1 + 0 = 3$

Add the parts:  $\frac{3}{5} + \frac{1}{2} + \frac{3}{4} = \frac{12}{20} + \frac{10}{20} + \frac{15}{20}$   
 $= \frac{37}{20}$   
 $= 1\frac{17}{20}$

Add the wholes and the parts:  $3 + 1\frac{17}{20} = 4\frac{17}{20}$

The children will make  $4\frac{17}{20}$  litres of purple paint.



I added all the fractions at once.





b) Paint needed for the roofs and the poles:  $3\frac{1}{2} + 1\frac{1}{5}$

Add the wholes:  $3 + 1 = 4$

Add the parts:  $\frac{1}{2} + \frac{1}{5} = \frac{5}{10} + \frac{2}{10} = \frac{7}{10}$

Add the wholes and the parts:  $4 + \frac{7}{10} = 4\frac{7}{10}$

Compare the fractions using equivalent fractions with a common denominator.

$$4\frac{7}{10} = 4\frac{14}{20}$$

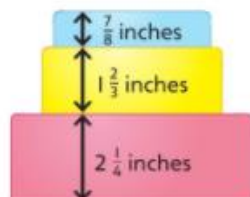
$4\frac{17}{20} > 4\frac{14}{20}$  so there will be enough purple paint to paint the roofs and the poles.

## Think together

1 Holly makes a wedding cake.

Calculate the total height of the cake using the two different methods.

The total height of the cake is   inches.



2 Work out the missing numbers.

a)   -  $2\frac{1}{3} = 1\frac{5}{6}$

b)  $2\frac{1}{3} - \frac{\text{input}}{\text{input}} = 1\frac{5}{6}$



3 Lee has some sheets of card.



Area =  $15\frac{4}{9} \text{ cm}^2$



Area =  $17\frac{1}{6} \text{ cm}^2$

Lee places the star on the blue card and sticks it down. What is the area of the blue background?



I think you need to add the areas together because you are putting them together.



I am not sure that is correct.



## Problem solving – adding and subtracting fractions 2

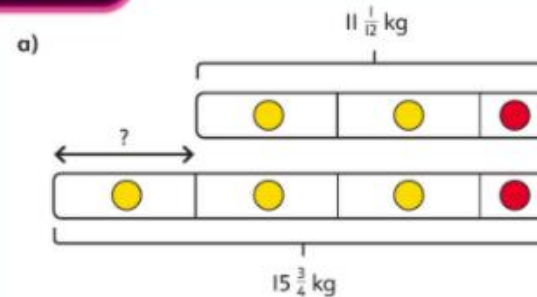


### Discover

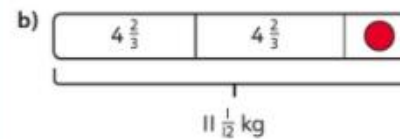


- 1** a) Aki's bowling balls have a total mass of  $15\frac{3}{4}$  kg.  
Bella's bowling balls have a total mass of  $11\frac{1}{12}$  kg.  
Work out the mass of one yellow ball.
- b) Work out the mass of one red striped ball.

### Share



Mass of 1 yellow bowling ball =  $15\frac{3}{4} - 11\frac{1}{12}$   
 $15\frac{3}{4} = 15\frac{9}{12}$   
 $15\frac{9}{12} - 11\frac{1}{12} = 4\frac{8}{12} = 4\frac{2}{3}$   
 The mass of 1 yellow bowling ball is  $4\frac{2}{3}$  kg.



The mass of 2 yellow bowling balls is  
 $4\frac{2}{3} + 4\frac{2}{3} = 8\frac{4}{3} = 8 + 1\frac{1}{3} = 9\frac{1}{3}$  kg  
 $11\frac{1}{12} = 10 + \frac{11}{12}$   
 So  $10\frac{11}{12} - 9\frac{1}{3} = 10\frac{11}{12} - 9\frac{4}{12} = 1\frac{7}{12}$   
 $1\frac{7}{12} = 1\frac{3}{4}$   
 The mass of one red striped bowling ball is  $1\frac{3}{4}$  kg.

I drew a bar model.  
I worked out the mass of one yellow bowling ball by subtracting.

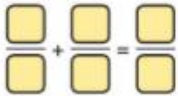


Now I know the mass of each yellow bowling ball I can put this into my model.



## Think together

- 1 What fraction of the shape is not shaded?



$\frac{3}{8}$  of the shape is not shaded.

- 2 Kate is cycling to the beach. It is  $6\frac{1}{3}$  km from her house. She cycles for  $2\frac{4}{5}$  km, has a break and then cycles for another  $1\frac{2}{3}$  km. How much further does she need to cycle?

- 3 Three points are marked on a number line.

C is  $1\frac{5}{6}$  less than B.

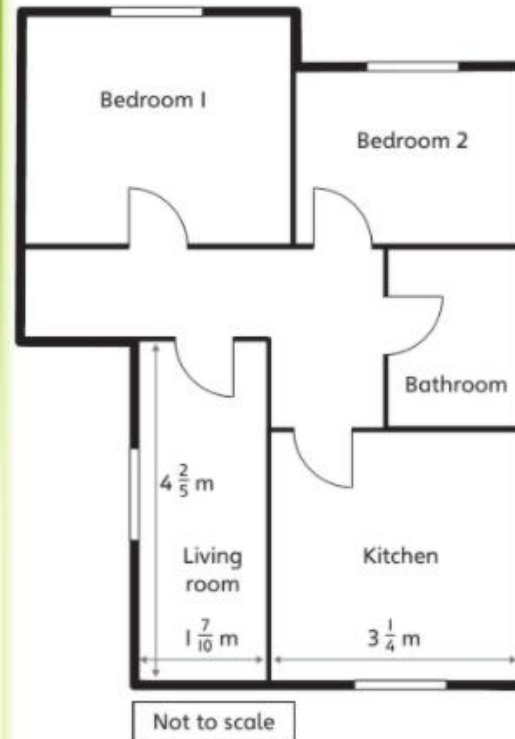


How much bigger is C than A?

- 4 Mo's house has a square shaped kitchen and a rectangle shaped living room.

Which room has the bigger perimeter?

How much bigger?



CHALLENGE

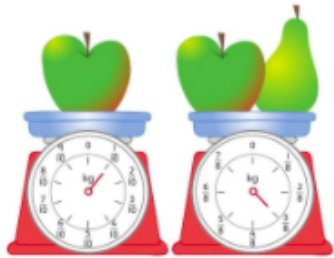
I must think what I know about squares and rectangles. I wonder if I have to add all four sides together to work out the answers.



# End of unit check

- 1 What is  $\frac{2}{3} + \frac{3}{5}$ ?
- A  $1\frac{4}{15}$       B  $1\frac{9}{15}$       C  $\frac{5}{8}$       D  $\frac{5}{15}$

- 2 How much does the pear weigh?



- A  $\frac{3}{8}$  kg      B  $\frac{11}{40}$  kg      C  $\frac{4}{18}$  kg      D  $\frac{19}{40}$  kg

- 3 Which one of these fractions is the biggest?

- A  $\frac{3}{4}$       B  $\frac{4}{5}$       C  $\frac{3}{5}$       D  $\frac{7}{10}$

- 4 What is  $2\frac{1}{5} + 3\frac{5}{6}$ ?



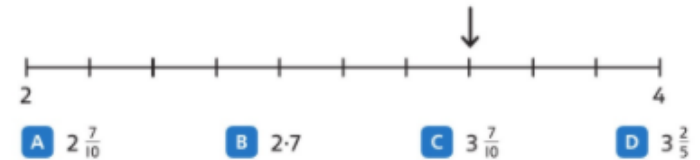
- A  $5\frac{6}{11}$       B  $5\frac{6}{30}$       C  $5\frac{1}{30}$       D  $6\frac{1}{30}$

- 5 What is the missing denominator?

$$1\frac{1}{4} + 1\frac{1}{\square} = 2\frac{9}{12}$$

- A 3      B 12      C 2      D 8

- 6 What is the number shown by the arrow?



- 7 At the school fete Lee is helping at the cake stall. He has  $3\frac{1}{2}$  cakes.



Lee sells  $2\frac{1}{6}$  cakes.

How many cakes does he have left?